Spectral signature of highly turbid waters
Application with SPOT data to quantify suspended particulate matter concentrations

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Abstract

An experimental method for determining water composition from “ocean colour” satellite data, in visible and near-infrared (NIR) wavelengths, is applied to highly turbid waters. Numerous spectroradiometric measurements are carried out in the Gironde estuary, for suspended particulate matter (SPM) concentrations ranging between 35 and more than 2000 mg l\textsuperscript{−1}. Empirical relationships are established between remote-sensing reflectance ($R_{rs}$) in SPOT-HRV bands and SPM concentration through these numerous in situ measurements. We observed that remote-sensing reflectance increases with SPM concentration and that the SPOT bands saturate at the highest turbidities. The best correlations are obtained for the NIR band XS3 (790–890 nm) and for the reflectance ratios: $R_{rs}(XS3)/R_{rs}(XS1)$ and $R_{rs}(XS3)/R_{rs}(XS2)$. The XS1 and XS2 visible bands are only used to determine SPM concentrations in the lower part of the estuary (where the SPM concentrations are lower). As a result, SPM concentrations within the surface waters in the estuary are estimated up to 2000 mg l\textsuperscript{−1} with an accuracy better than ±35%. The algorithm is finally applied to a SPOT scene. Satellite data are corrected for atmospheric effects using a radiative transfer code and in situ reflectance measurements; as a result, the horizontal distribution of SPM is retrieved. Moreover, the high spatial resolution HRV-SPOT sensor shows detailed sedimentary flows, especially in the visible XS1 and XS2 spectral bands. © 2002 Elsevier Science Inc. All rights reserved.

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1. Introduction

In clear oceanic Case 1 waters (Morel & Prieur, 1977), algorithms are used to interpret satellite data in terms of chlorophyll concentration (O’Reilly et al., 1998), and hence, deduce primary production (Antoine, Morel, & André, 1995; Morel, 1988). The signal becomes more complicated in coastal and estuarine Case 2 waters where terrestrial substances, such as coloured dissolved organic matter (CDOM or yellow substances) and suspended particles, are present in addition to phytoplankton. In these turbid waters, incident light scattering by suspended particulate matter (SPM), and therefore the attenuation of light within the water column, is important (Gordon & McCluney, 1975; Ivanoff, 1975; Morel, 1991). Therefore, SPM has an inhibitive effect on primary production in coastal waters and its detection is essential in understanding biological mechanisms. The quantification of SPM is also necessary to design dredging strategies on navigational channels and to estimate the fluvial solid discharges to the ocean.

The interpretation of satellite imagery in coastal Case 2 areas often involves the calculation of empirical relationships between the parameters of interest and in situ optical measurements. In this way, numerous studies have looked at turbid plumes (e.g., Anji Reddy, 1993; Forget & Ouillon, 1998; Froidefond, Castaing, Mirmand, & Ruch, 1991; Ouillon, Forget, Froidefond, & Naudin, 1997; Siegel, Gerth, & Mutzke, 1999) and have quantified (to an appropriate precision) the fluvial suspended matter discharges to the ocean. Recent works have

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attempted to derive SPM concentrations, and hence, fluxes in estuaries (Moore, Aiken, & Lavender, 1999; Robinson, Morris, & Dyer, 1998); the results are encouraging, but significant effort is required to reduce the retrieval uncertainty (about ±50%).

The Gironde estuary (southwest France) is an extreme example of Case 2 waters, as SPM concentrations in surface waters can reach more than 2 g/l. The objective is to determine SPM concentrations with high-resolution remotely sensed data, in order to quantify the sedimentary fluxes and to improve the validation of two hydrodynamic and transport numerical models recently adapted to the estuary (Sottolichio, Le Hir, & Castaing, 2001).

In situ spectroradiometric measurements, carried out since 1996, constitute an important optical database that will aid in the understanding of coastal waters. The in situ optical measurements include the remote-sensing reflectance \( R_{rs, s} \) defined as (Mobley, 1999) (Eq. (1)):

\[
R_{rs, s} = \frac{L_w}{E_d},
\]

where \( L_w \) (W m\(^{-2}\) sr\(^{-1}\) nm\(^{-1}\)) is the water-leaving radiance and \( E_d \) (W m\(^{-2}\) nm\(^{-1}\)) is the downwelling irradiance incident on the water surface. These in situ spectra were used to establish algorithms to quantify SPM concentrations in the Gironde estuary. Particular care was taken to correct for the skylight reflection, which perturbs above-water surface radiometric measurements. Algorithms were applied to a SPOT scene, according that SPOT-HRV high-spatial resolution imagery is suitable for monitoring small-scale areas. The three spectral bands are: XS1 (500–590 nm) and XS2 (610–680 nm) visible wavelengths, XS3 (790–890 nm) NIR wavelengths.

2. The study area

The Gironde estuary (Fig. 1), southwest France, gives a good example of sediment-dominated Case 2 waters influenced by river inputs. The origin of the particles is twofold: the two rivers’ (Garonne and Dordogne) inputs and erosion of recently settled sediments by tidal currents (Castaing, 1981). The suspended matter is a mixture of organic and mineral composites, where the organic fraction represents only 1.8% of the total material (Jouanneau & Latouche, 1981). The mineral fraction is composed of micas (63%) and quartz (25%), while clay phases contain four minerals: montmorillonite (30%), illite and interstratified minerals (40%), kaolinite (15%), chloride and interstratified minerals (15%). The grain-size distribution is:

- <2 \( \mu m \): 47%;
- 2–15 \( \mu m \): 40%;
- 16–63 \( \mu m \): 9%;
- > 63 \( \mu m \): 4% (Jouanneau & Latouche, 1981).

Recent measurements, in the Gironde mouth (Weber, Jouanneau, Ruch, & Mirmand, 1991), showed that a mean grain-size varied between 7.1 and 12.7 \( \mu m \). The dimensions of the flocculated particles, 1 m below the water surface, were measured by Eisma et al. (1991) with a system of video cameras. The mean diameter, practically independent of SPM concentration, was around 120 \( \mu m \). Moreover, the nature and grain-size of the particles vary little with the seasons (Castaing, 1981; Eisma & Li, 1993). Chlorophyll-\( a \) (Chl-\( a \)) and CDOM concentrations are low, with Chl-\( a \) ranging from 1 to 3 mg l\(^{-1}\) (Irigoien & Castel, 1997), and dissolved organic carbon (DOC) ranging from 1 to 7 mgC l\(^{-1}\) (Abril et al., 1999).

The Gironde estuary has well-developed turbidity maximum, with both tidal asymmetry and density residual circulation involved in its formation (Castaing & Allen, 1981). The estimated total sediment mass in the turbidity maximum/fluid mud system is about 5 \times 10^6 tons, which represents 2 years of riverine solid input (Jouanneau & Latouche, 1981). The high-turbidity zone is characterised by mean SPM concentrations of about 1 g/l (Allen, Salomon, Bassoulet, Du Penhoat, Degranpré, 1980; Allen, Sauzay, Castaing, & Jouanneau, 1977) and recent numerical simulations (Sottolichio et al., 2001) clearly demonstrated the tidal origin of the turbidity maximum. Salinity-induced density effects (Sottolichio et al., 2001) probably do not contribute to its formation, but they appear essential to retain SPM in the lower parts of the estuary and maintain the stable mass of the turbidity maximum.
3. Measurements

3.1. In situ measurements

In situ measurements were carried out in the estuary during the SEDIGIR (21st June, 29th June, and 22nd July 1996), PNOCTEL-97 (from 23rd June to 1st July 1997) oceanographic surveys. Above-water radiance measurements have been taken since 1996 in the estuary to validate ocean colour satellite data, with a co-incident water sample for each optical measurement. The optical sensor is a Spectron SE-590 spectroradiometer, with a high-resolution recorder and acceptance angle of 6°. A water sample is taken at a depth of between 0 and 1 m. SPM concentration is determined by filtering the water sample on Whatman GF/F glass-fibre filters (diameter: 47 mm; pore size: 0.44 μm).

The sensor was placed 3 m above the surface while measuring \( L_u \) and 20 cm above the Spectralon plate when measuring \( L_d \).

The plate is a Lambertian target for solar zenith angles (\( \theta_s \)) between 0° and 40°, as its reflectance varies by only 3% (Dilligeard, 1997). In these conditions, the downwelling irradiance \( E_d (\mu W m^{-2} nm^{-1}) \) is given by the following relationship (Eq. (2)):  
\[
E_d(\lambda) = \pi \frac{1}{R_p(\lambda)} L_d(\lambda),
\]

where \( \lambda (nm) \) is the wavelength.

The total remote-sensing reflectance \( T_{ru} (sr^{-1}) \) is then calculated as follows (Eq. (3)):  
\[
T_{ru}(\lambda) = R_p(\lambda) \frac{L_u(\lambda)}{\pi L_d(\lambda)} = \frac{L_u(\lambda)}{E_d(\lambda)}.
\]

Above-water radiances \( L_u(\lambda) \) were corrected for skylight reflection effects (sky glint) as a part of the incident light is directly reflected by the air–water interface (Fougnie, Frouin, Lecomte, & Deschamps, 1999; Mobley, 1999). The above-water radiance \( L_u(\lambda) \) is therefore (Mobley, 1999) (Eq. (4)):  
\[
L_u(\lambda) = L_w(\lambda) + L_r(\lambda),
\]

where \( L_w \) is the water-leaving radiance and \( L_r \) is the sky radiance directly reflected by the surface. \( L_r \) can be estimated from sky radiance (\( L_s \)) measurements (Mobley, 1999):  
\[
L_r = \rho L_s,
\]

where \( \rho \) is a proportional factor which relates the sky radiance (\( L_s \)) to the radiance directly reflected by the surface (\( L_r \)). The water-leaving radiance (\( L_w \)) is then (Eq. (6)):  
\[
L_w(\lambda) = L_u(\lambda) - \rho L_s(\lambda).
\]

The \( \rho \) value was assumed to be wavelength-independent and the value 0.02 (Austin, 1974) was considered. In fact, the \( \rho \) factor varies with viewing geometry, sky conditions (clear, cloudy, overcast), sea surface roughness (depending on wind), and is wavelength-dependent under a cloudy sky (Fougnie et al., 1999; Mobley, 1999). Mobley used radiative transfer code to estimate cloud effects on \( \rho \) value, for uniform sky radiance distribution and for a wind speed of 10 m s\(^{-1}\). He obtained a \( \rho \) value of 0.337 for a clear sky, a \( \rho \) value depending on wavelength for a sky with a single cumulus cloud \( [\rho(XS1)=0.0392, \rho(XS2)=0.0452, \rho(XS3)=0.0635] \).

The influence of skylight reflection can be estimated from typical in situ measurements of upwelling and sky radiance (\( L_u \) and \( L_s \) in \( \mu W m^{-2} sr^{-1} nm^{-1} \)) (integration time of 4/64 s), carried out under a clear blue sky on 21st July 2000 at 12:35 (local time) where the SPM concentration was 158 mg l\(^{-1}\). As the water surface was flat, the four consecutive \( L_u \) measurements are practically identical. Between 400 and 1000 nm, sky radiance is low in NIR wavelengths (700–1000 nm), moderate in red wavelengths (600–700 nm), and reaches its maximum in green–yellow wavelengths (450–550 nm). According to Eq. (5) and in situ measurements of sky radiance (Fig. 3), the skylight reflection effects were minima in the NIR band (XS3),...
Fig. 3. Upwelling and sky radiance \( L_u(\lambda) \) and \( L_s(\lambda) \) in \( \mu W \, m^{-2} \, sr^{-1} \, \mu m^{-1} \) measurements carried out at Pauillac, on 21st July 2000 at 12:35 (local time), under a clear blue sky. SPM concentration is 158 mg l\(^{-1}\).

## 3.2. Satellite data and atmospheric corrections

A SPOT scene was acquired on 14th July 1996 at 11:23 UT and covers the whole estuary. For each band, Eq. (10) was used to convert the digital numbers (DNs) into radiance units (Eq. (7)):

\[
L^* = \frac{DN}{A_k}
\]

where \( L^* (W \, m^{-2} \, sr^{-1} \, \mu m^{-1}) \) is the top of atmosphere (TOA) upwelling radiance and \( A_k \) (\( W^{-1} \, m^2 \, sr \, \mu m \)) is the calibration factor for spectral band \( k \), given by SPOT-Image.

\( L^* \) was converted to TOA reflectance, \( R^* \) (unitless) using the following relationship (Vermote, Tanre, Deuze, Herman, & Morcrette, 1997) (Eq. (8)):

\[
R^*(XSi) = \frac{\pi L^*(XSi)}{\mu s E_s(XSi)},
\]

where \( i = 1, 2, \) or 3 for XS1, XS2, XS3; \( \mu_s = \cos(\theta_s) \), \( \theta_s \) is the solar zenith angle; \( E_s(XSi) \) (W m\(^{-2}\) \( \mu m \)) is the solar TOA irradiance (1865, 1615, and 1090 W m\(^{-2}\) \( \mu m \) in channel XS1, XS2, and XS3, respectively).

The TOA measurements were then corrected for atmospheric effects using the 6s radiative transfer simulation software (Vermote et al., 1997). \( R^* \) is related to the above-water reflectance \( R_{aw} \) (unitless) following the relationship (Eq. (9)):

\[
R^* = T_g [R_{aw} + R_{ray} + T_d R_w],
\]

where \( R_{aw} \) and \( R_{ray} \) (unitless) are the aerosol and Rayleigh reflectances, respectively; \( T_g \) and \( T_d \) (unitless) are the gaseous and diffuse transmittances, respectively.

### Table 1

Upwelling radiance \( L_u \) and sky radiance \( L_s \) recorded at Pauillac, 21st July 2000 at 12:35 (local time), in SPOT spectral bands (XS1, XS2, and XS3)

<table>
<thead>
<tr>
<th>SPOT spectral band</th>
<th>XS1</th>
<th>XS2</th>
<th>XS3</th>
</tr>
</thead>
<tbody>
<tr>
<td>( L_u ) (W m(^{-2}) sr(^{-1}) ( \mu m^{-1} ))</td>
<td>398.54</td>
<td>425.93</td>
<td>97.92</td>
</tr>
<tr>
<td>( L_s ) (W m(^{-2}) sr(^{-1}) ( \mu m^{-1} ))</td>
<td>260.42</td>
<td>129.54</td>
<td>29.58</td>
</tr>
</tbody>
</table>

#### Austen, 1974

\( (\rho_L)/(\rho_s) \) (%)

<table>
<thead>
<tr>
<th>( (\rho_L)/(\rho_s) ) (%)</th>
<th>( \rho )</th>
<th>( \rho )</th>
<th>( \rho )</th>
</tr>
</thead>
<tbody>
<tr>
<td>(clear sky)</td>
<td>(0.0337)</td>
<td>0.0392</td>
<td>0.0452</td>
</tr>
<tr>
<td>(single cumulus cloud)</td>
<td>0.0635</td>
<td>0.0635</td>
<td>0.0635</td>
</tr>
</tbody>
</table>

The \( (\rho_L)/(\rho_s) \) values represent the percentage of total measured upwelling radiance \( L_u \) due to sky radiance \( (\rho_s) \). Percentages are calculated for \( \rho \) values determined by Mobley (1999) for different sky conditions: (a) clear sky \( \rho = 0.0337 \); sky with single cumulus cloud \( \rho(XS1) = 0.0392 \), \( \rho(XS2) = 0.0452 \), \( \rho(XS3) = 0.0635 \); Percentage errors committed when considering the Austen (1974) \( \rho \) value are noted in parentheses.
The final atmospherically corrected reflectance ($R_{ac}$, unitless) is:

$$R_{ac} = \frac{R_w}{1 + SR_w},$$

where $S$ (unitless) is the total spherical albedo.

This atmospherically corrected reflectance, divided by $\pi$ steradians, can be compared to the remote-sensing reflectance: $1/\pi R_{sr}(\lambda) \approx R_{ac}(\lambda)$.

Atmospheric effects take into account gaseous (oxygen, ozone, water vapour, etc.) transmittance, molecular scattering and extinction (Rayleigh), aerosol scattering and extinction. The 6s model also corrects for skylight reflection (Sun glint and sky glint) following the Snell–Fresnel laws, environmental effects, and directional target effects.

In order to estimate the atmospheric composition over the study area, at the moment of the satellite’s overpass, an appropriate atmospheric model was selected: the “midlatitude summer” standard model, which defines pressure (mb), temperature (K), water vapour and ozone densities (g m$^{-3}$) as functions of altitude (km). Of the three predefined tropospheric aerosol models (Continental, Maritime, and Urban), a model with 90% continental and 10% maritime aerosols was selected as it took into account the eastern winds blowing from the land.

The aerosol optical thickness (at 550 nm) is obtained by integrating the total extinction coefficient, $K_{550}$ (km$^{-1}$) (Eq. (11)):

$$\tau(550) = \int_0^\infty K_{550}(z)dz. \quad (11)$$

The total extinction coefficient is defined as (Eq. (12)):

$$K_{550}(z) = \sigma_{550} 10^{-3} N(z) \quad (12)$$

where $\sigma_{550}$ ($\mu$m$^{-2}$) is the extinction cross-section and the aerosol density ($N$, part./cm$^3$) is a function of visibility ($v$, km) (Eq. (13)):

$$N(z) = \frac{a(z)}{v} + b(z), \quad (13)$$

where $z$ is the altitude (km). This relationship was determined by McClatchey, Fenn, Selby, Volz, and Garing (1971), with $a(z)$ and $b(z)$ expressed in part./cm$^3$ and part./cm$^2$, respectively.

In this research, the visibility measurements were obtained from the national meteorology survey (METEO-FRANCE) at Bordeaux-Mérignac airport, 20 km far from the study area.

In situ reflectance measurements were used to improve and validate the atmospheric corrections. Target areas, with known in situ reflectances, were identified on the imagery; they are Médoc beaches and Hourtin lake, located to the west of the estuary (Fig. 1). Following Chavez’s (1988) method, the lake is considered as a black target in the SPOT-XS3 band. The visibility value, and therefore aerosol optical thickness, is adjusted until the atmospherically corrected NIR reflectance was zero. The beaches have very high reflectances in the HRV-SPOT bands. Atmospherically corrected reflectances were compared to in situ reflectance values.

In Fig. 4, TOA reflectances are plotted versus atmospherically corrected reflectances, corresponding to corrections established for the SPOT image taken on 14/07/96. The relationships are almost linear in each SPOT spectral band, as the atmosphere is considered homogenous and as the correction of skylight reflection is uniform over the whole estuary (small-scale reflection effects, resulting from surface roughness, are consequently neglected).

4. Spectral reflectance model

4.1. Theory

Interpretation of remote-sensing reflectance measurements as a function of water composition necessitates to relate $R_{ns}$ to inherent optical properties (IOPs) of the water body.

$R_{ns}$ can be written as a function of the irradiance reflectance just beneath the surface ($R$), according to (Morel & Gentili, 1993):

$$R_{ns} = \frac{(1 - \rho)(1 - \bar{\rho}) R}{n^2 (1 - \bar{\rho} R)} \bar{Q}, \quad (14)$$

where (Morel & Gentili, 1996): $\rho$, the internal Fresnel reflectance, is equal to 0.021 for $\theta = 0$; $\bar{\rho}$, the air–water Fresnel reflection at the interface, typically amounts between 4% and 5%; $n$, is the refractive index of water ($= 1.34$); $\bar{Q}$, the water–air reflection, is of the order of 0.48; $R$, the reflectance or irradiance reflectance, is defined as the ratio $E_d(0-)/E_d(0-)$, with $E_d(0-)$ and $E_d(0-)$ the upwelling and downwelling irradiances at null depth.
denoted \( 0; Q = E_d(0) / L_d(0) \), in steradians, would be \( \pi \) if the \( L_d \) distribution was isotropic, but may vary between approximately 3.1 and 5.6.

The dimensionless reflectance \( (R) \) can be related to the IOPs of the water body according to (Gordon, Brown, & Jacobs, 1975) (Eq. (15)):

\[
R = \frac{b_b}{a + b_b} 
\]

where \( f \) is a coefficient varying with illumination conditions and water types, \( a \) (m\(^{-1}\)) and \( b_b \) (m\(^{-1}\)) are the absorption and backscattering coefficients of the water body, respectively. The commonly adopted value for \( f \) is the mean value 0.33, which is valid for zenith Sun and large variety of naturals waters (Morel & Prieur, 1977).

The ratio \((1 - p)/(1 - R)\) accounts for all the reflection and refractive effects at the air–water interface. \((1 - p)/(1 - R)\) is approximately equal to 0.54 when \( \theta = 0 \). For Case 1 waters where reflectance \( (R) \) is lower than 0.1, the term \((1 - R)\) is generally assumed to be unity. For Case 2 waters, \( R \) is generally higher than 0.1 and the term \((1 - R)\) must be considered. Therefore, an approximate formulation of Eq. (14) is (Eq. (16)):

\[
R_{rs} \approx \frac{0.54}{1 - 0.48 \times 0.33 \frac{b_b}{a + b_b}} \frac{b_b}{Q \frac{a + b_b}{a + b_b}} = \frac{0.18}{1 - 0.16 \frac{b_b}{a + b_b}} \frac{b_b}{Q \frac{a + b_b}{a + b_b}}. \tag{16}
\]

It indicates that \( R_{rs} \) is a function of \( Q^{-1} \) (which accounts for the bidirectional effects; Morel & Gentili, 1996) and \([b_b/(a + b_b)]\) (which accounts for the IOPs).

### 4.2. Reflectance model

A spectral (400–900 nm) reflectance model, presented by Forget, Ouillon, Lahet, and Broche (1999) for sediment-dominated Case 2 waters influenced by river inputs, is adapted to the Gironde estuarine waters, in order to better interpret our in situ measurements, i.e., to estimate the effects of turbidity; the absorption and backscattering coefficients, which are expressed as the sum of contributions from optically active constituents. Only contributions of sediments and yellow substance are considered, assuming that contribution of phytoplankton to reflectance is very small. The absorption and backscattering coefficients are written (Eqs. (17) and (18)):

\[
a(\lambda) = a_w(\lambda) + a_y(\lambda) + a_s(\lambda) \tag{17}
\]

\[
b_b(\lambda) = b_{bw}(\lambda) + b_{bs}(\lambda) \tag{18}
\]

where subscripts \( w, y, \) and \( s \), respectively, stand for water, yellow substance, and sediment. Absorption by sediments was neglected by Forget et al. (1999), but is considered in this study as SPM concentration in the Gironde estuary is extremely high.

Values of \( a_w(\lambda) \) are taken from Smith and Baker (1981) for the range 400–800 nm and are deduced from Hale and Querry (1973) for the range 800–900 nm. \( a_y(\lambda) \) is modelled by (Bricaud, Morel, & Prieur, 1981) (Eq. (19)):

\[
a_y(\lambda) = a_y(\lambda_0) \exp[-s(\lambda - \lambda_0)] \tag{19}
\]

where wavelengths are expressed in nanometers, \( \lambda_0 = 440 \) nm, \( s = 0.014 \) nm\(^{-1}\).

Absorption by sediments is modelled by (Bricaud & Stramsky, 1990):

\[
a_s(\lambda) = a_s(\lambda_0) \exp[-k(\lambda - \lambda_0)] \tag{20}
\]

where \( \lambda_0 = 440 \) nm, \( k \) varies in the range 0.005–0.009 nm\(^{-1}\) and the 0.009 is arbitrarily taken. \( a_s(\lambda_0) \) is expressed as a function of SPM concentration (Cipollini & Corsini, 1994):

\[
a_s(\lambda_0) = 0.042*(\text{SPM}/S), \text{ where } S \text{ is a constant value (}=3.327) \text{ (Schnitz-Pieffer, Viehoff, & Grassl, 1990).}
\]

\[
b_{bs}(\lambda) \text{ is equal to one-half the total scattering coefficient } b_s(\lambda) \text{ (Morel, 1980) for the range 400–800 nm and is neglected at greater wavelengths. Light scattering by suspended particles is modelled using the Mie theory (Van de Hulst, 1957), which allows to express } b_{bs}(\lambda) \text{ by (Forget et al., 1999):}
\]

\[
b_{bs}(\lambda) = \frac{3\text{SPM}}{2\rho_{\text{SPM}} \ln(\frac{D_{\text{max}}}{D_{\text{min}}})} \int_{D_{\text{min}}}^{D_{\text{max}}} Q_{bs}(D, m_r, \lambda) D^{-2} dD \tag{21}
\]

where \( \rho_{\text{SPM}} \) is the sediment density, \( D \) the diameter of sediment particles, and \( Q_{bs} \) the backscattering efficiency factor of sediment particles of refractive index \( m_r \).

A Junge particle size distribution of slope-4 (Nanu & Robertson, 1993) is assumed for the wide range of diameters 0.01–120 \( \mu \)m (\( D_{\text{min}} - D_{\text{max}} \)), which include fine and flocculated particles. The sediment density is assumed to be 2600 kg m\(^{-3}\). The refractive index of sediment particles is taken in the range 1.10–1.15, with a mean value of 1.125.

### 5. Results

#### 5.1. Spectral signature of highly turbid waters

In situ optical measurements provide spectral signatures of Gironde estuarine waters of various SPM concentrations. Fig. 5 displays some typical remote-sensing reflectance (\( R_{rs} \)) spectra measured in 1996 and 1997. The following conclusions can be drawn: between 400 and 1000 nm, \( R_{rs} \) increases with turbidity; the maximum \( R_{rs} \) value increases from 0.028 sr\(^{-1}\) (SPM concentration of 35 mg l\(^{-1}\)) to...
0.078 sr\(^{-1}\) (1797 mg l\(^{-1}\)); the wavelength maximum increases from green to red and NIR wavelengths with increasing SPM concentration. From 35 to 250 mg l\(^{-1}\), the reflectance increases between 400 and 700 nm and then, beyond 250 mg l\(^{-1}\), the reflectance tends to saturate at these wavelengths, but strongly increases between 750 and 950 nm. A second \(R_{rs}\) maximum appears at 800 nm, that is characteristic of highly turbid waters as it was not yet observed in the Gironde plume, where SPM concentrations are lower (Froidefond et al., 1991). Reflectance is far from zero in the NIR (950–1000 nm) and clearly depends on SPM concentration.

According to Eq. (14), \(R_{rs}\) is a function of the IOPs, expressed by the ratio \(\frac{b}{a+b}\). This ratio is modelled for a constant yellow substance concentration, expressed as \(a_y(440\text{ nm})\). \(a_y(440\text{ nm})\) is taken equal to 0.6 m\(^{-1}\), which is representative of most of estuarine waters (Kirk, 1983). Variations of \(\frac{b}{a+b}\) with wavelengths are computed for SPM concentrations of 35, 82, 248, 326, 783, and 1797 mg l\(^{-1}\) (Fig. 6). The maximum ratio value, obtained when SPM concentration is 1797 mg l\(^{-1}\), is lower than 0.25 which involves the term \((1 - \hat{r} \frac{b}{a+b})\) varies in the range of 0.96–1, with a mean value of 0.98 (with \(\hat{r} = 0.48\) and \(f = 0.33\)). Eq (14) can be rewritten:

\[
R_{rs} \approx \frac{0.178}{0.98} \frac{b}{a+b} = 0.182 \frac{b}{Q(a+b)}.
\]

Comparison between the computed \(\frac{b}{a+b}\) ratio (Fig. 6) and some of typical measured \(R_{rs}\) spectra (Fig. 5) shows that the adopted model parameters are approximate but realistic, and clearly demonstrates the predominant influence of the IOPs, which involves that variations due to bidirectional aspects are weak. As a consequence, most of variations observed on \(R_{rs}\) spectra can be explained with the considered reflectance model.

### 5.2. Empirical relationships

In 1996 and 1997, several \(R_{rs}\) measurements (42 in total) were taken in the estuary and related to SPM concentrations between 35 and 2072 mg l\(^{-1}\). The \(R_{rs}(\lambda)\) spectra were converted into SPOT equivalent remote-sensing reflectances \(R_{rs}(XS1), R_{rs}(XS2),\) and \(R_{rs}(XS3)\). In total, the 42 points
were used to develop empirical SPM algorithms in the concentration range 35–2072 mg l\(^{-1}\). The relationships corresponding to XS1, XS2, and XS3 are presented in Figs. 7, 8, and 9, respectively, where the plotted curves are the best correlated functions between 35 and 500 mg l\(^{-1}\). The legend on the graphs indicates the date of measurements.

For XS1 (Fig. 7), the reflectance first increases with increasing SPM concentration, quickly reaches a maximum level (0.062 sr l\(^{-1}\) for 300 mg l\(^{-1}\)), then the signal becomes strongly variable (between 0.030 and 0.062 sr l\(^{-1}\)) independently of SPM concentration and finally seems to decrease at extreme turbidity. A linear relationship is observed in the lowest concentrations (SPM < 50 mg l\(^{-1}\)), which is in agreement with results obtained by Froidefond et al. (1991). Between 35 and 500 mg l\(^{-1}\), a logarithmic relationship with a correlation coefficient of .58 is found:

\[
R_{rs}(XS1) \times 100 = 0.0631 + 0.7662 \times \ln(\text{SPM}).
\]

No acceptable correlation is found for the whole concentration range. For XS2 (Fig. 8), the reflectance is proportional to SPM at concentrations of up to 100 mg l\(^{-1}\), reaches a maximum around 300 mg l\(^{-1}\), then saturates and even decreases at extreme turbidities. Between 35 and 500 mg l\(^{-1}\), a logarithmic relationship with a correlation coefficient of .63 is found:

\[
R_{rs}(XS2) \times 100 = 0.9200 + 1.2587 \times \ln(\text{SPM}).
\]

The reflectance variations, as a function of SPM concentration, are similar in the two visible spectral bands (XS1 and XS2): a logarithmic increase up to 500 mg l\(^{-1}\), before saturation. The best correlation is found for XS3 (Fig. 9). The NIR reflectance is proportional to SPM concentration up to 500 mg l\(^{-1}\), then decreases until 1300 mg l\(^{-1}\) and finally reaches a maximum value (around 0.07 sr l\(^{-1}\)) for the highest concentrations (SPM >1500 mg l\(^{-1}\)). From 35 to 500 mg l\(^{-1}\), the linear increase (plotted on the graph) is:

\[
R_{rs}(XS3) \times 100 = 0.7633 + 0.0093 \times \text{SPM},
\]

with a correlation coefficient of .75. This relationship is in agreement with Moore et al. (1999) where the reflectance in MERIS band 14 (865 nm) was measured for fine sediment from the Humber estuary (UK) under laboratory conditions.

Skylight reflection does not significantly affect in situ measurements in SPOT spectral bands and the observed relationships are mainly due to the IOPs, expressed as the \([b/(a+b)]\) ratio. In order to explain \(R_{rs}\) variations in SPOT bands, the \([b/(a+b)]\) ratio is modelled in XS1, XS2, and XS3 for SPM concentration ranging from 25 to 2000 mg l\(^{-1}\). Three refractive indexes of sediment particles (\(m_r\)) are considered (1.10, 1.125, and 1.15) to estimate the model sensitivity.

---

**Fig. 9.** Reflectance in XS3 band \(R_{rs}(XS3) \times 100\) versus SPM concentration. Between 0 and 500 mg l\(^{-1}\), the function is linear with a correlation factor of .924 (\(a=0.156, b=0.008\)).

**Fig. 10.** Computed 0.33 \([b/(a+b)]\) ratio in XS1 band versus pseudo-SPM concentration, for three values of the sediment refractive index \(m_r\). Values of other model parameters: \((D_{min}, D_{max})= (0.1, 120) \mu m; a_y (440 nm)=0.6 \text{ m}^{-1}\).

**Fig. 11.** Computed 0.33 \([b/(a+b)]\) ratio in XS2 band versus pseudo-SPM concentration, for three values of the sediment refractive index \(m_r\). Values of other model parameters: \((D_{min}, D_{max})= (0.1, 120) \mu m; a_y (440 nm)=0.6 \text{ m}^{-1}\).
The modelled \([b_b/(a+b_b)]\) ratio increases from SPM concentration of 25 to 250 mg l\(^{-1}\) in XS1 band (Fig. 10), from 25 to 500 mg l\(^{-1}\) in XS2 (Fig. 11), then saturates for higher SPM concentrations, independently of \(m_r\). In the XS3 band, \([b_b/(a+b_b)]\) increases with SPM concentration from 25 to 2000 mg l\(^{-1}\) (Fig. 12). Analysis of computed \(a\), \(b_b\), \(a_s\), and \(b_{bs}\) coefficients (Table 2) shows that contribution of pure water to light backscattering can be neglected for the considered SPM concentration (>25 mg l\(^{-1}\)), which involves: \(b_b \approx b_{bs}\). A second observation is that contribution of pure water and yellow substance to light absorption becomes insignificant in XS1 and XS2, when SPM concentration is higher than 250 and 500 mg l\(^{-1}\), respectively, which involves \(a \approx a_s\). In XS3, absorption by pure water is always predominant compared to absorption by sediments. When contribution of pure water and yellow substance to light absorption is significant, the \([b_b/(a+b_b)]\) ratio can be written:

\[
\frac{b_b}{a + b_b} = \frac{b_{bs}}{(a_s + a_y)} + \frac{a_s + b_{bs}}{(a_s + b_{bs})} \quad (23)
\]

According to Eqs. (20) and (21), \(a_s(\lambda\) and \(b_{bs}(\lambda)\) are both proportional to SPM concentration, and can be written: \(a_s(\lambda) = \text{SPMf}_1(\lambda); b_{bs}(\lambda) = \text{SPMf}_2(\text{SPM.D}.m_r,\lambda)\), where \(f_1\) and \(f_2\) are functions independent of SPM concentration. Eq. (23) becomes (Eq. (24)):

\[
\frac{b_b}{a + b_b} = \frac{\text{SPMf}_2}{(a_s + a_y) + \text{SPM}(f_1 + f_2)} \quad (24)
\]

It explains why the \([b_b/(a+b_b)]\) ratio, and therefore the \(R_{es}\) measurements, increases with increasing SPM concentration in XS1 (25 < SPM < 250 mg l\(^{-1}\)), in XS2 (25 < SPM < 500 mg l\(^{-1}\)) and in XS3 (25 < SPM < 2000 mg l\(^{-1}\)).

When contribution of pure water and yellow substance to light absorption becomes insignificant, the \([b_b/(a+b_b)]\) ratio can be written (Eq. (25)):

\[
\frac{b_b}{a + b_b} = \frac{b_{bs}}{a_s + b_{bs}} = \frac{\text{SPMf}_2}{\text{SPM}(f_1 + f_2)} = \frac{f_2}{f_1 + f_2} \quad (25)
\]

The \([b_b/(a+b_b)]\) ratio, and therefore the \(R_{es}\) measurements, becomes independent of SPM concentration, which explains the saturations observed in XS1 (SPM >250 mg l\(^{-1}\)) and in XS2 (SPM >500 mg l\(^{-1}\)).

The computed \([b_b/(a+b_b)]\) ratio in XS1, XS2, and XS3 is highly sensitive to variations of \(m_r\). The range of particle grain-size \((D_{min} - D_{max})\), which was supposed invariant in our computations, is another sensitive model parameter (Forget et al., 1999). The variations of \(m_r\) and \((D_{min} - D_{max})\), which probably occurred during our in situ measurements, can explain irregularities observed in Figs. 7–9.

Changes in sediment composition and grain-size, which directly influence \([b_b/(a+b_b)]\) and \(R_n\) in a single band through the \(b_{bs}\) coefficient, can be reduced when considering reflectance ratios (Moore et al., 1999). In fact, assuming that \(b_b \approx b_{bs}\) for SPM concentration greater than 25 mg l\(^{-1}\) and that spectral variations of \(b_{bs}\) are weak, the ratio \(\frac{R(XS3)}{R(XS1)} = \frac{(b_b/(a+b_b))(XSI)/(b_b/(a+b_b))(XS3)}{(a(XS1) + b_{bs}(XSI))/(a(XS3) + b_{bs}(XS3))}\) (where \(i = 1\) for XS1 and \(i = 2\) for XS2) is written (Eq. (26)):

\[
\frac{R(XS3)}{R(XS1)} \approx \frac{b_{bs}(XS3)}{b_{bs}(XS1)} \frac{a(XS1) + b_{bs}(XSI)}{a(XS3) + b_{bs}(XS3)}
\]

The contribution of the \(b_{bs}\) coefficient to \(\frac{R(XS3)}{R(XS1)}\) ratios is limited. As a result, when the computed \(\frac{R(XS3)}{R(XS1)}\) and \(\frac{R(XS2)}{R(XS1)}\) ratios are plotted versus SPM concentration (Figs. 13 and 14), it appears that influence of \(m_r\) variations

![Fig. 13. Computed \([b_b/(a+b_b)](XS3)/(b_b/(a+b_b)(XS1))\) ratio versus pseudo-SPM concentration, for three values of the sediment refractive index \(m_r\). Values of other model parameters: \((D_{min}, D_{max})=(0.1, 120)\) μm; \(a_y\) (440 nm) = 0.6 m\(^{-1}\).](image-url)
are notably reduced. According to Eq. (22), remote-sensing reflectance ratios are written (Eq. (27)):

\[
\frac{R_{rs}(X_{S3})}{R_{rs}(X_{Si})} = \frac{Q(X_{S3})}{Q(X_{Si})} \frac{R(X_{Si})}{R(X_{S3})}
\] (27)

Consequently, these \( R_{rs} \) ratios will be seldom affected by variations of \( m_r \). This assumption is confirmed by in situ \( R_{rs} \) measurements: the \([R_{rs}(X_{S3})/R_{rs}(X_{S1})]\) (Fig. 15) and \([R_{rs}(X_{S3})/R_{rs}(X_{S2})]\) (Fig. 16) ratios are well correlated to SPM concentration. Moreover, the obtained relationships include all in situ measurements completed during the different field campaigns within the \( \pm 0.011 \text{ sr}^{-1} \) (Fig. 15) and \( \pm 0.007 \text{ sr}^{-1} \) (Fig. 16) function uncertainties. The influence of particle grain-size and refractive index variations, which directly affect reflectance in SPOT bands, is therefore reduced when considering reflectance ratios. Comparison between the measured \( R_{rs} \) ratios (Figs. 15 and 16) and the modelled \( R \) ratios (Figs. 13 and 14), plotted versus SPM concentration, confirms once again that variations of the \( Q \) function are weak. The established relationship (Fig. 15) is written:

\[
\frac{R_{rs}(X_{S3})}{R_{rs}(X_{S1})} = 0.3193\ln(\text{SPM}) - 0.9614
\] (28)

with a correlation factor of .9306. The function is logarithmic between 35 and 2250 mg l\(^{-1}\) and shows a linear increase in this ratio at SPM concentrations lower than 500 mg l\(^{-1}\), then a more moderate increase for higher concentrations (from 500 to 2250 mg l\(^{-1}\)).

The second relationship (Fig. 16):

\[
\frac{R_{rs}(X_{S3})}{R_{rs}(X_{S2})} = 0.1884\ln(\text{SPM}) - 0.4832
\] (29)

has a correlation factor of .9147. The function is also logarithmic; a linear increase is observed for the lower concentrations.

### Table 3

| SPM concentrations determined from the \([R_{rs}(X_{S3})/R_{rs}(X_{S1})]\) reflectance ratio |
|-----------------------------------|---------------------------------|-----------------|-----------------|-----------------|-----------------|
| Mean SPM concentration (mg l\(^{-1}\)) | Minimum SPM concentration (mg l\(^{-1}\)) | Maximum SPM concentration (mg l\(^{-1}\)) | Uncertainty (%) |
| 0.2 | 38 | 28 | 53 | 32.9 |
| 0.3 | 52 | 37 | 73 | 34.6 |
| 0.4 | 71 | 51 | 100 | 34.5 |
| 0.5 | 97 | 69 | 137 | 35.0 |
| 0.6 | 133 | 95 | 187 | 34.6 |
| 0.7 | 182 | 130 | 255 | 34.3 |
| 0.8 | 249 | 176 | 350 | 34.9 |
| 0.9 | 340 | 241 | 480 | 35.1 |
| 1.0 | 465 | 330 | 656 | 34.9 |
| 1.1 | 635 | 451 | 900 | 35.3 |
| 1.2 | 870 | 617 | 1228 | 35.1 |
| 1.3 | 1187 | 842 | 1680 | 35.3 |
| 1.4 | 1627 | 1155 | 2297 | 35.1 |
| 1.5 | 2225 | 1578 | 3135 | 35.0 |

The given mean, minimum, and maximum SPM (mg l\(^{-1}\)) and the percentage error (%) are deduced from the uncertainties presented in Fig. 8.

Fig. 15. \( R_{rs}(X_{S3})/R_{rs}(X_{S1}) \) band ratio versus SPM concentration. The function is logarithmic (second rate) with a correlation factor of .935 (\(a = -0.5014, b = 0.03983\)).
concentrations (SPM < 500 mg l$^{-1}$), then the increase is logarithmic and finally, the reflectance ratio reaches its maximum value of 0.9.

These empirical relationships are obtained with high correlation coefficients (>0.9) and the ±0.011 and ±0.007 sr$^{-1}$ and include most points, independently of the date of measurement. They are consequently robust to determine SPM concentrations from above-water reflectance measurements, at least for the period covered by the field campaigns (1996 and 1997 summers). The percentage errors associated with the retrieved SPM concentrations from Eq. (28) (Table 3) and Eq. (29) (Table 4) are lower than 38%.

5.3. SPM concentrations

From all in situ measurements completed in 1996 and 1997 summers, a single relationship was obtained between SPM concentration and the reflectance band ratio $[R_{rs(XS3)}/R_{rs(XS2)}]$. This relationship is consequently valid at least for the 1996 and 1997 summer periods and can be applied to a SPOT scene taken during this time, even if no in situ measurements were performed during the satellite overpass.

The algorithm is applied to the SPOT image taken on the 14th of July 1996. Satellite data recorded in XS2 and XS3 bands are corrected for atmospheric effects. Reflectance band ratio $[R_{rs(XS3)}/R_{rs(XS2)}]$ values are converted to SPM concentrations according to Eq. (29) (Fig. 16). SPM concentrations are quantified with uncertainties indicated (Table 4). Only the downstream part of the estuary is presented (Fig. 17) and the geographical borders of the area are defined in Fig. 1.

The imagery was acquired during a period of low river flow and according to the sedimentology knowledge of the estuary (Castaing, 1981; Sottolichio et al., 2001), the turbidity maximum would have been located between Pauillac and Bordeaux (Fig. 1).

At image acquisition time, the upstream and central parts of the estuary (PK 20–PK 70) were influenced byebb tide currents and the downstream part (PK 70–PK 90) had a slack tide, with the flood tide starting in the mouth.

SPM concentrations, detected from satellite data (Fig. 17), decrease from upstream to downstream (from the right to the left on the image), ranging from more than 700 mg l$^{-1}$ to approximately 20 mg l$^{-1}$. The highest SPM concentrations are found along the navigation channel (C) and right-hand shore banks (D) where ebb tide currents reach their maximum velocity, erode recently settled sediment, and transport it downstream. The lowest concentrations (SPM < 100 mg l$^{-1}$) are located in the downstream part of the estuary: the slow (slack tide) currents cannot transport suspended particles, which fall and settle. The flood tide, starting near the mouth, brings clear oceanic water into the estuary. The Talais and Marguerites banks (A and B) have high SPM concentrations (around 300 mg l$^{-1}$), which probably result from resuspension over shallow waters. Downstream, along the estuary shore, underwater mud banks appear as clear areas (F).

These observations are in good agreement with previous knowledge of the estuarine sedimentology (Castaing, 1981; Sottolichio et al., 2001) and tidal data. The navigation channel is easily located and starts with a stretched turbulent flow created by the strong ebb current (C). Progressively, the flow widens with decreasing current velocity (E), and follows the channel morphology. Upstream, sedimentary flows are longitudinal and parallel to the shore, as a result of strong ebb currents that transport SPM from the turbidity maximum towards the centre and downstream parts of the estuary.

Table 4

<table>
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<tr>
<th>$R_{rs(XS3)}/R_{rs(XS2)}$</th>
<th>Mean SPM concentration (mg l$^{-1}$)</th>
<th>Minimum SPM concentration (mg l$^{-1}$)</th>
<th>Maximum SPM concentration (mg l$^{-1}$)</th>
<th>Uncertainty (%)</th>
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</table>

The given mean, minimum, and maximum SPM (mg l$^{-1}$), and the percentage error (%) are deduced from the uncertainties presented in Fig. 9.
Downstream, flows are wider, moving slowly towards the right-hand shore. Oceanic clear water intrusions at the mouth are opposed to the declining sedimentary flows. The features observed within the shallow waters, over mud banks and sandbanks (A and B) and along the shorebanks (D) probably result from resuspension.

6. Discussion and conclusions

An experimental methodology was used to interpret “ocean colour” satellite data of highly turbid waters, the Gironde estuary, and a relationship between remote-sensing reflectance and SPM concentration was established. The satellite data were corrected for atmospheric effects, using radiative transfer code and in situ reflectance measurements, and then converted to SPM concentrations.

The main advantage of the method is the direct comparison of in situ radiometric measurements (radiance or equivalent remote-sensing reflectance) and the concentrations of optically active substances, but it requires an accurate knowledge of the water body and sufficient in situ measurements. The in situ measurements describe the spectral variation of remote-sensing reflectance $R_{rs}(\lambda)$ with SPM: $R_{rs}(\lambda)$ increases with SPM concentration, first at the lower wavelengths (400–600 nm), then in the middle wavelengths (600–700 nm), and finally, in the NIR domain (700–900 nm); a characteristic maximum reflectance appears at 800 nm.

The methodology was applied to the Gironde estuary, using HRV-SPOT data. The SPOT visible band (XS1 and XS2) reflectances were poorly correlated with SPM, but showed a logarithmic increase up to 500 mg l$^{-1}$ and then saturation. This result indicated that the skylight reflection effects were significant, but the IOPs mainly influenced the relationships. The $R_{rs}(\text{XS3})$ band, the $R_{rs}(\text{XS3})/R_{rs}(\text{XS1})$ ratio, and the $R_{ds}(\text{XS3})/R_{ds}(\text{XS2})$ ratio were highly correlated with SPM concentration. The use of remotely sensed reflectance ratios reduced skylight reflection and was therefore used instead of a single band. As a result, SPM was quantified to a high precision (±35%).

The SPOT-HRV data showed detailed sedimentary flows in the estuary, with the suspended particles acting as excellent currents markers, as the mean settling velocity was low (about 1 mm/s). The particle’s capability to backscatter incident light in visible and NIR wavelengths produced strong reflectance signals, and therefore, high SPM concentrations appeared as bright areas in the image.

In conclusion, sedimentary flows are predominant features in the estuary and move within the surface waters; SPOT data can be used to rapidly locate the turbidity maximum, erosion and deposition areas; suspended particles can act as currents markers, providing observations of hydrodynamic features.

Future developments include improvements to the atmospheric correction: the inclusion of small-scale reflection effects (induced by the surface roughness) and Rayleigh/aerosol interaction. The methodology will also be applied to Landsat-7 data, which have seven spectral bands in the visible and infrared wavelengths, and a high spatial resolution suitable to estuaries. Supplementary homogeneous targets near the Gironde estuary will be used to improve and validate the atmospheric corrections.

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References


