A reflectance band ratio used to estimate suspended matter concentrations in sediment-dominated coastal waters

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Abstract. This letter presents an empirical relationship that may be used to estimate the suspended particulate matter concentrations in highly turbid waters from remote sensing reflectance measurements. Numerous measurements carried out in the Gironde estuarine waters (France) in 2000 and 2001 are presented and analysed. It was observed that the near-infrared (850 nm) reflectance was weakly correlated with the total suspended matter concentration (TSMc) measured in surface waters. A strong correlation ($r = 0.91$) was obtained between the ratio of the near-infrared and visible (550 nm) reflectance and $TSMc$, which could provide an accurate calibration curve for data from Système Probatoire de l'Observation de la Terre (SPOT), Landsat and Indian Remote Sensing (IRS) satellite sensors. The reflectance ratio reduced the effects of changes in illumination conditions and sediment type (grain-size, refractive index). The calibration function obtained, successfully applied to the Gironde, should be applied in other sediment-dominated coastal waters.

1. Introduction

One of the applications of visible and near-infrared remote sensing in oceanography is to relate the measured water-leaving signal to the constituents of the waterbody (e.g. phytoplankton, dissolved organic matter, mineral particles). With remotely sensed imagery, the process generally includes a preliminary correction for atmospheric effects. Then, theoretical or empirical algorithms may be used to derive information about water constituents (optical properties, concentrations) from the estimated water-leaving signal. Considering sediment-dominated coastal waters, refined algorithms are needed to estimate accurately the suspended particulate concentrations from ocean colour remotely sensed data (e.g. Bowers et al. 1998, Robinson et al. 1998, Froidefond et al. 1999, Moore et al. 1999) notably to provide calibration data for numerical hydro-sedimentary models (Siegle et al. 1999). The objective in this study is to develop such an inversion algorithm, which could permit the accurate estimation of the total suspended matter concentration ($TSMc$) distributions from remotely sensed data, independently of the date of acquisition. The aim is to provide a calibration function relating reflectance to $TSMc$ in spectral bands of actual and future fine spatial resolution satellite sensors.

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2. Theory

The remote sensing reflectance signal ($R_{rs}$ in sr$^{-1}$) is defined by (Mobley 1994)

$$R_{rs} = \frac{L_w}{E_d}$$  \hspace{1cm} (1)

where $L_w$ (in Wm$^{-2}$ sr$^{-1}$ nm$^{-1}$) is the water-leaving radiance and $E_d$ (in Wm$^{-2}$ nm$^{-1}$) is the downwelling irradiance.

According to Morel and Gentili (1996), the above water $R_{rs}$ signal can be expressed as a function of the irradiance reflectance ($R$, unitless) at null depth, noted $0^-$ ($R = [E_u(0-)/E_d(0-)]$, with $E_u$ the upwelling irradiance)

$$R_{rs} = \frac{0.529}{(1 - \bar{r}R)} \frac{R}{Q}$$  \hspace{1cm} (2)

where the term 0.529 results of the air–water Fresnel reflection and refraction effects for the remote sensing configuration, $\bar{r}$ is the water–air reflection and is of the order of 0.48, $Q$ is the upwelling irradiance to upwelling radiance ratio $[E_u(0-)/L_u(0-)]$ (in sr) which would be $\pi$ if the $L_u$ distribution were isotropic, but may vary between approximately 3.1 and 5.6.

The irradiance reflectance is written as a function of the inherent optical properties (IOPs) of the waterbody, namely the absorption and backscattering coefficients $a$ and $b_b$ (in m$^{-1}$), according to (Gordon et al. 1975)

$$R = f' \frac{b_b}{a + b_b}$$  \hspace{1cm} (3)

where the value of $f'$ is 0.324 for a Sun close to the zenith (Morel and Gentili 1996). Thus, the remote sensing reflectance is finally written

$$R_{rs} = 0.529 \frac{a + b_b}{a + (1 - \bar{r}f')b_b} \frac{f'}{Q} \frac{b_b}{a + b_b} = 0.529 \frac{f'}{Q} \frac{b_b}{a + (1 - \bar{r}f')b_b}$$  \hspace{1cm} (4)

which indicates its dependence on the IOPs and, according to Morel and Gentili (1993), on the illumination conditions and viewing directions through the $f'$ and $Q$ parameters.

3. Field measurements

Data were collected in the Gironde estuary during two successive summers (July and September 2000; July, August and September 2001) at four fixed stations located in the border of the main navigation channel, at the following distances from Bordeaux: 30, 52, 67 and 85 km (figure 1).

Optical data were recorded with a Spectron SE-590 spectroradiometer with 256 sensors in the interval 400–1100 nm (band width: 2.8 nm per sensor), following the measurement procedure described by Doxaran et al. (2002). The radiometer was directed vertically toward the water, 1 m above the surface, when measuring the upwelling radiance $L_u$, vertically directed toward a spectrallon target when measuring the downwelling radiance $L_d$ and directed toward the zenith when measuring the sky radiance $L_s$. The target is near Lambertian for solar zenith angles between 0–40°, as its reflectance ($R_p$) varies by only 3% (Dilligeard 1997). In these conditions, the downwelling irradiance $E_d$ was ($\pi L_d/R_p$). Upwelling radiance measurements were
Figure 1. The Gironde estuary, located in south-west France. The lines represent the main navigation channels. Black circles locate the four fixed stations of field measurements.

corrected for skylight reflection effects (sky glint) by subtracting 2% of the measured sky radiance (Austin 1974), in order to estimate the water-leaving radiance (Mobley 1999). The measured remote sensing reflectance was finally given by

$$R_{rs} = R_p \frac{L_u - 0.02 L_s}{\pi L_d}.$$  \hspace{1cm} (5)

For each optical measurement, the $TSMc$ was measured near the surface (50 cm depth) by filtering a water sample on Whatman GF/F glass-fibre filters (diameter 47 mm, pore size 0.44 μm).

Field measurements were carried out when there was a clear blue sky (no cloud) and a quasi-plane water surface (wind speed close to 0 m s$^{-1}$). A total of 34 coincident $R_{rs}$ and $TSMc$ [in the range (0.013–0.985 g l$^{-1}$)] data samples, recorded in July 2000 (18 and 21 July 2000, four samples), September 2000 (25–29 September 2000, 22 samples), July 2001 (4 July 2001, one sample), August 2001 (25 August 2001, two samples) and September 2001 (10–13 September 2001, five samples), were available.

The measured $R_{rs}$ typically increased with $TSMc$ in the range 400–1000 nm, notably at 550 and 850 nm which are the central wavelengths of Système Probatoire
de l’Observation de la Terre–High Resolution Visible (SPOT-HRV) and Landsat-Advanced Thematic Mapper (ETM) + yellow-green and near-infrared spectral bands, respectively (figure 2). The largest increase was observed in the near-infrared wavelengths (700–900 nm) where $R_{rs}$ was practically zero for a low $TSMc$ (0.013 g l$^{-1}$) and was about 0.1 sr$^{-1}$ for a high $TSMc$ (0.985 g l$^{-1}$).

4. Results and discussion

Variations of the $R_{rs}$ signal measured at 550 nm and 850 nm, denoted $R_{rs}(550)$ and $R_{rs}(850)$, were observed as a function of $TSMc$. As expected, $R_{rs}(850)$ increased with increasing $TSMc$ in the range 0.010–0.250 g l$^{-1}$ ($r = 0.79$) (figure 3). Over 0.25 g l$^{-1}$, $R_{rs}(850)$ tended to saturate. Concerning the visible wavelength, no significant correlation was found between $R_{rs}(550)$ and $TSMc$ (results are not presented here), which could lead to the following conclusion: reflectance measurements in visible and near-infrared bands do not allow an accurate estimation of $TSMc$.

It was observed that the reflectance ratio $[R_{rs}(850)/R_{rs}(550)]$ was strongly correlated to $TSMc$ ($r = 0.91$) (figure 4). Values were close to zero for the lowest $TSMc$ (<0.050 g l$^{-1}$) as $R_{rs}(850)$ was close to zero, then rose to 110% for the highest $TSMc$. The error associated with each $R_{rs}$ measurement depends on the residual error committed when correcting the measured $L_u$ signals for skylight reflection effects. This residual error cannot be assessed from the data. However, it was observed that if a ±7% uncertainty is assumed for the $[R_{rs}(850)/R_{rs}(550)]$ ratio, the polynomial function plotted on the graph ($R^2 = 0.97$) includes all data collected in 2000 and 2001. This function allows an accurate estimation of $TSMc$ from $R_{rs}$ measurements.

To explain the obtained results, refer to equation (4) which indicates that $R_{rs}$ is a function of both geometrical parameters, namely $f'$ and $Q$, and of the IOPs, namely $a$ and $b^b$.

The measurements were carried out for different tidal conditions (neap/spring tides) independently of the tidal cycle (ebb/flood tides, low/high water periods) and at different locations in the estuary. Consequently, they probably correspond to a variety of sediment grain-size and refractive index. Results of computations with an

![Figure 2. Examples of measured $R_{rs}$ spectra for different $TSMc$: a, 0.013 g l$^{-1}$; b, 0.023 g l$^{-1}$; c, 0.062 g l$^{-1}$; d, 0.355 g l$^{-1}$; e, 0.651 g l$^{-1}$; and f, 0.985 g l$^{-1}$.](image)
Figure 3. $R_{ss}$ measured at 850 nm plotted against $TSMc$. Date of measurements: July (rhombus), August (circles) and September (squares) 2000 (grey points) and 2001 (black points). Plot of the second order polynomial regression. Plot of the function uncertainty including points in the range 0.01–0.25 g l$^{-1}$.

Figure 4. Ratio of reflectance $[R_{ss}(850 nm)/R_{ss}(550 nm)]$ plotted against $TSMc$. Date of measurements: July (rhombus), August (circles) and September (squares) 2000 (grey points) and 2001 (black points). Plot of the third order polynomial regression and the $\pm 7\%$ reflectance ratio uncertainty which includes all points in the range 0.010–1.000 g l$^{-1}$.

IOP model (Lahet 1999) have shown that the backscattering coefficient by sediment is highly dependent on the sediment type (grain-size, refractive index). Doxaran et al. (2002) have integrated these results into a reflectance model adapted to the Gironde estuary and observed that these variations of sediment type highly influence the
$R_{rs}(850)$ signal, independently of the sediment concentration. Moreover, as illustrated by Morel and Gentili (1996), the $f'/Q$ ratio depends on the illumination conditions (i.e. the solar zenith angle). As a conclusion, a part of the variations of the measured $R_{rs}(850)$ signal (figure 3) was probably due to sediment type and solar zenith angle variations which occurred during the field campaigns.

According to equation (4), a ratio of the near-infrared ($\lambda_1$) and visible ($\lambda_2$) remote sensing reflectance can be approximately written

$$R_{rs}(\lambda_1)/R_{rs}(\lambda_2) = \left[ \frac{f'}{Q}(\lambda_1) / \frac{f'}{Q}(\lambda_2) \right] \left\{ \frac{b_b(\lambda_1) a(\lambda_2) + (1 - \bar{r} f'(\lambda_2)) b_b(\lambda_2)}{b_b(\lambda_2) a(\lambda_1) + (1 - \bar{r} f'(\lambda_1)) b_b(\lambda_1)} \right\}$$

Doxaran et al. (2002) showed that the ratio within braces [equation (6)] weakly depends on sediment type variations which induce variations of the $bb$ coefficient; and is highly correlated with TSMc. Morel and Gentili (1993, 1996) showed that, for unvarying optical properties of a given water body, spectral variations of the $f'/Q$ ratio are low, which could lead to a simplification of equation (6): $[(f'/Q)(\lambda_1)/f'(\lambda_2)] \approx 1$. No measurements of the $f'$ and $Q$ were carried out during the field campaigns, but the relationships obtained tend to confirm this assumption. In fact, the [$R_{rs}(850)/R_{rs}(550)$] reflectance ratio was highly correlated to TSMc, and depends weakly on illumination conditions and sediment type variations which occurred during the field measurements (figure 4). The relationship obtained plotted on the graph (figure 4) will permit the development of an invariant algorithm used to estimate the TSMc in the Gironde estuary from remotely sensed data.

5. Conclusion
From numerous field reflectance measurements, an empirical relationship was established which allows the accurate estimation of suspended particulate matter concentrations in the Gironde estuary. This relationship is based on a simple reflectance ratio between near-infrared (850 nm) and visible (550 nm) wavelengths. While reflectance in the near-infrared allowed only an approximate estimation of TSMc between 0.015–0.250 g L$^{-1}$, a high correlation coefficient ($r = 0.91$) was obtained between this ratio and TSMc, including all measurements collected during two successive low river flow periods on 2000 and 2001 and providing an accurate estimation of TSMc up to 0.500 g L$^{-1}$. The empirical relationship obtained confirmed the results obtained by Doxaran et al. (2002) using a reflectance model adapted to the Gironde estuary: the use of reflectance ratios between near-infrared and visible wavelengths reduces and even partly eliminates the effects of sediment type (grain-size, refractive index) variations occurring during regular field reflectance measurements.

To determine the limits of the established relationship, it will be applied to other measurements for the Gironde estuary and for other sites. Results should permit the development of original inversion algorithms based on reflectance ratios for SPOT, Landsat and Indian Remote Sensing satellite (IRS) sensors, in sediment-dominated coastal waters.

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